**Topics: Normal distribution, Functions of Random Variables**

1. The time required for servicing transmissions is normally distributed with *μ* = 45 minutes and *σ* = 8 minutes. The service manager plans to have work begin on the transmission of a customer’s car 10 minutes after the car is dropped off and the customer is told that the car will be ready within 1 hour from drop-off. What is the probability that the service manager cannot meet his commitment?
2. 0.3875
3. 0.2676
4. 0.5
5. 0.6987

Ans - Since work begins after 10 minutes after the car is dropped, the time left to complete the work is 50 minutes. The probability that the service manager not meet his commitment = P(X>50) = 1-P(x<=50) (X is the time taken to complete the work). Convert 50 into Z-score.

Standard normal variable = (X –mu)/sigma = (x-45)/8

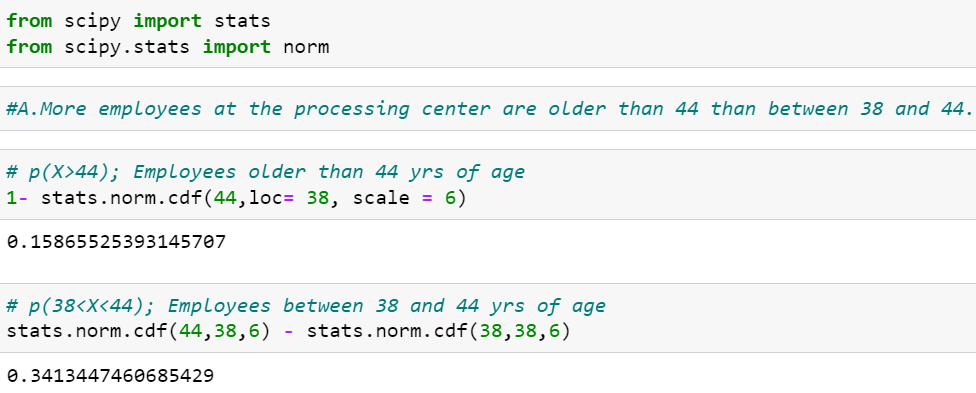
P(X<=50) = P(Z<=(50-45)/8) = PR(Z<=0.625)= 0.73237 = 73.237% (the number in z-table)

The probability that the service manager cannot meet his commitment is 100-73.237 =

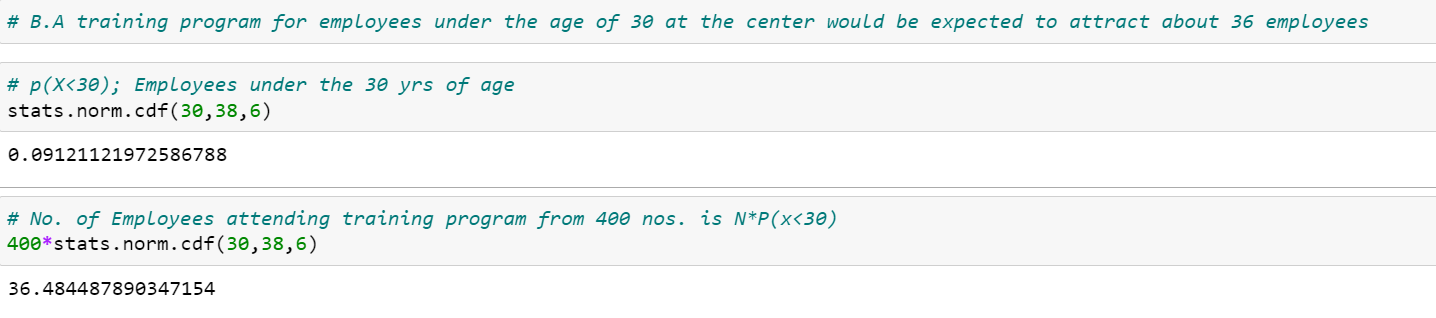
26.763% = 0.2676

So, answer is B

1. The current age (in years) of 400 clerical employees at an insurance claims processing center is normally distributed with mean *μ* = 38 and Standard deviation *σ* =6. For each statement below, please specify True/False. If false, briefly explain why.
2. More employees at the processing center are older than 44 than between 38 and 44.



1. A training program for employees under the age of 30 at the center would be expected to attract about 36 employees.



1. If *X1* ~ *N*(μ, σ2) and *X*2 ~ *N*(μ, σ2) are *iid* normal random variables, then what is the difference between 2 *X*1 and *X*1 + *X*2? Discuss both their distributions and parameters.

Ans - we know that if X ∼ N(µ1, σ1^2 ), and Y ∼ N(µ2, σ2^2 ) are two independent random variables then X + Y ∼ N(µ1 + µ2, σ1^2 + σ2^2 ) , and X − Y ∼ N(µ1 − µ2, σ1^2 + σ2^2 ) .

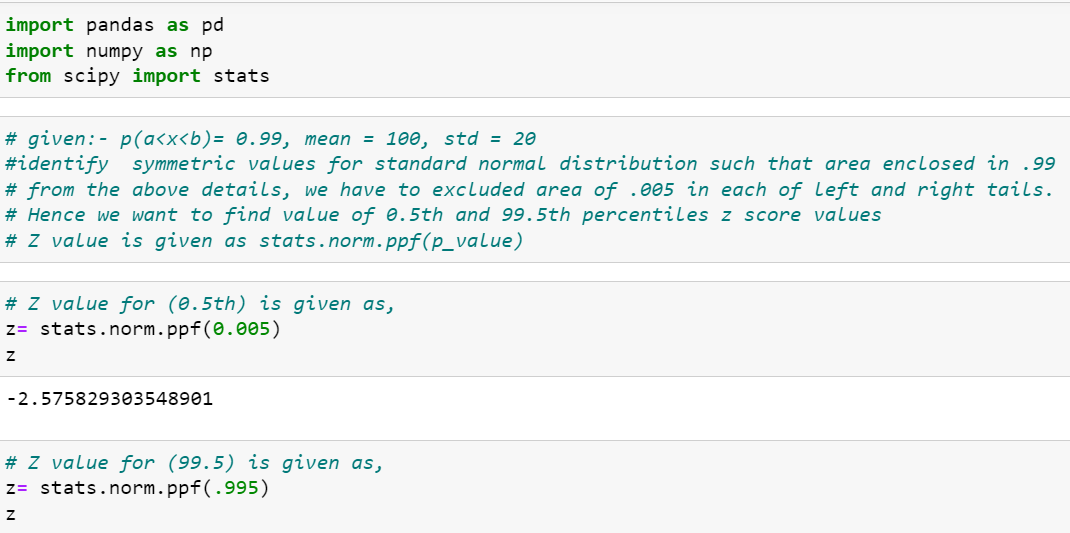
Similarly if Z = aX + bY, where X and Y are as defined above, Similarly if Z = aX + bY , where X and Y are as defined above,

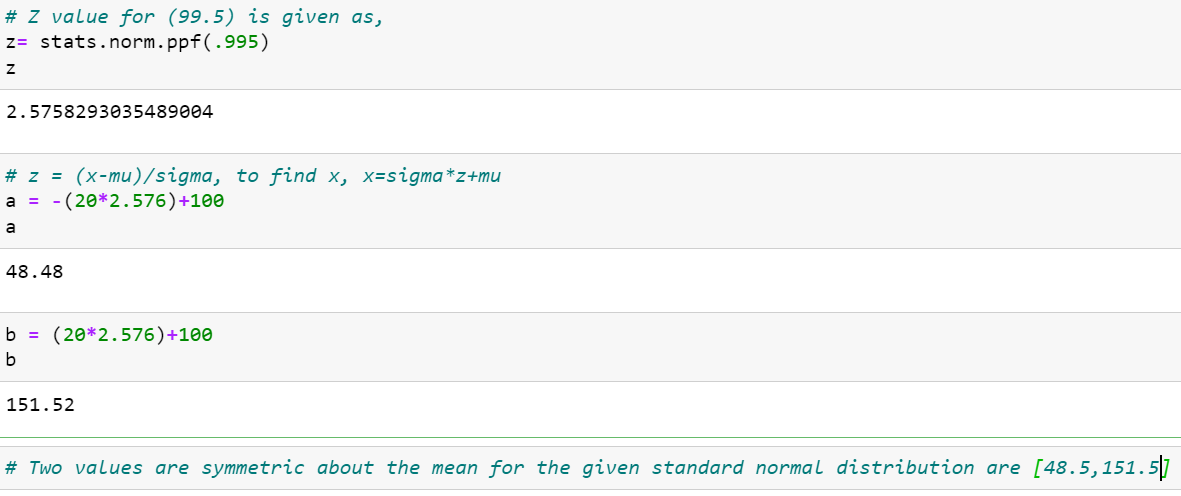
Therefore in the question,

X1~ N(2 u,4 σ^2) and X1+X2 ~ N(µ + µ, σ^2 + σ^2 ) ~ N(2 u, 2σ^2)

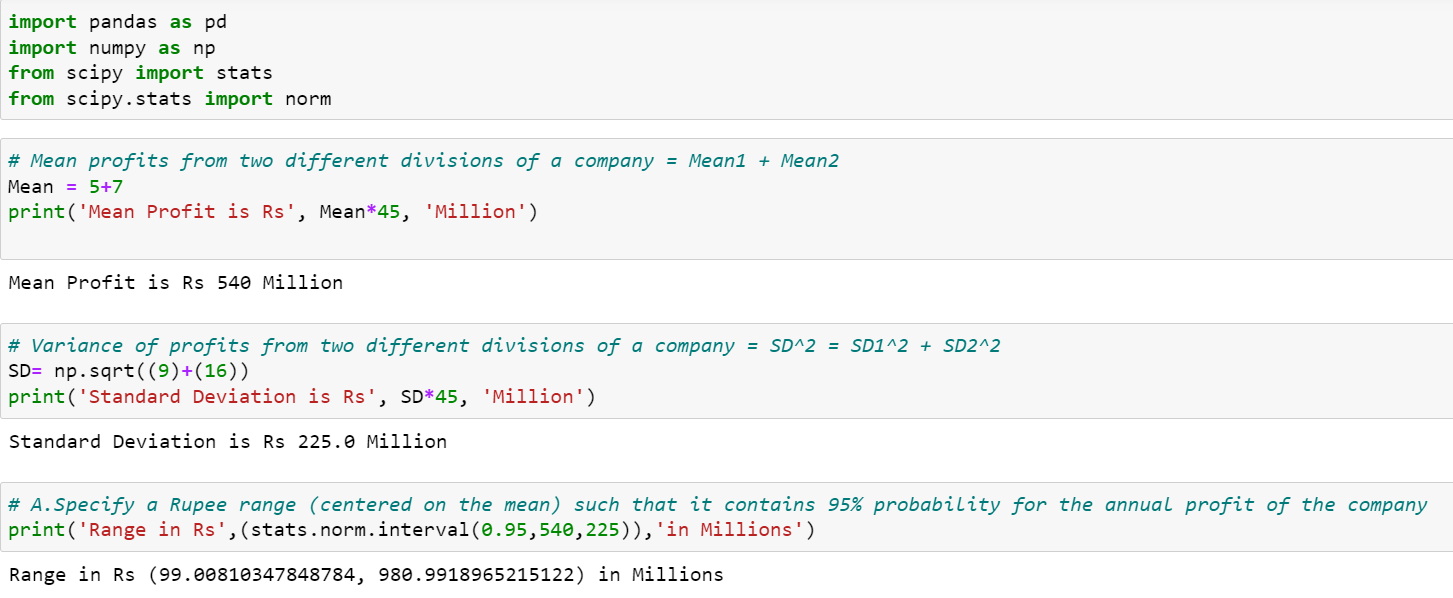
2X1-(X1+X2) = N(4µ,6 σ^2)

1. Let X ~ N (100, 202). Find two values, *a* and *b*, symmetric about the mean, such that the probability of the random variable taking a value between them is 0.99.
2. 90.5, 105.9
3. 80.2, 119.8
4. 22, 78
5. 48.5, 151.5
6. 90.1, 109.9

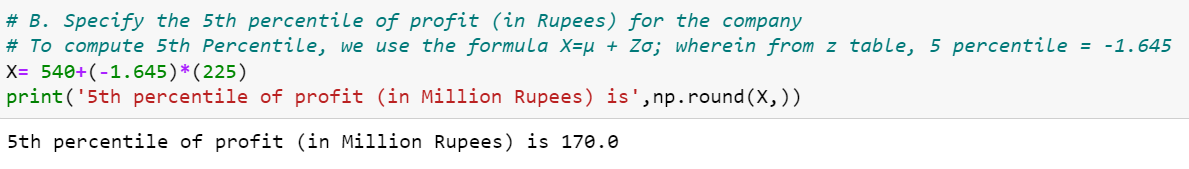
Ans - 



1. Consider a company that has two different divisions. The annual profits from the two divisions are independent and have distributions Profit1 ~ N(5, 32) and Profit2 ~ N(7, 42) respectively. Both the profits are in $ Million. Answer the following questions about the total profit of the company in Rupees. Assume that $1 = Rs. 45
2. Specify a Rupee range (centered on the mean) such that it contains 95% probability for the annual profit of the company.



1. Specify the 5th percentile of profit (in Rupees) for the company



1. Which of the two divisions has a larger probability of making a loss in a given year?

